

Pontryagin's principle for some robust optimal control problems

Hasnaa Zidani, INSA Rouen Normandie, France

Contact: Hasnaa.Zidani@insa-rouen.fr

In this talk, we present a class of control problems with uncertainties. Let T be a given finite horizon, and let $(\Omega, \mathcal{F}, \mathbb{P})$ be a complete probability space. Consider an ensemble of controlled state equations parametrized by the random variable $\omega \in \Omega$:

$$\begin{cases} \dot{\mathbf{x}}_\omega(t) = A\mathbf{x}_\omega(t) + B(\omega)\mathbf{u}(t) + f(t, \omega) & \text{for a.e. } t \in [0, T], \\ \mathbf{x}_\omega(0) = x_0, \\ \mathbf{u}(t) \in U, & \text{for a.e. } t \in [0, T], \end{cases} \quad (1)$$

where U is a closed metric space, x_0 is an initial data, A and $B(\omega)$ are linear operators in appropriate spaces (of finite or infinite dimension), and f is a smooth source term. An admissible control input $u : [0, T] \rightarrow H$ is a measurable function assumed to be ω -independent, which means that the *parametrized family of states* are driven by the same control. The optimal control problem is as follows

$$\text{Maximize } \{\mathbb{P}(\Psi(\mathbf{x}_\omega(T)) \leq 0) \mid (\mathbf{x}_\omega, \mathbf{u}) \text{ satisfies (1)}\}$$

where $\Psi : H \rightarrow \mathbb{R}$ is a given function. The cost function evaluates the probability that the ensemble of controlled states verify a constraint at the final time.

In this talk, we will discuss the optimality conditions of the robust control problem and show that these conditions can be expressed as a Pontryagin principle.

This is a joint work with W. van Ackooij (EDF Lab, France) and R. Henrion (Wias, Berlin)